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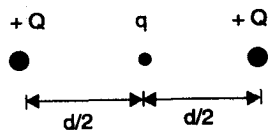
MARKS: 180

**ELECTROSTATICS**

**LEVEL - II**

1. Two positively charged particles each having charges  $Q$  are  $d$  distance apart. A third charge is introduced in midway on the line joining the two. Find nature and magnitude of third charge, so that the system is in equilibrium:

- a)  $q = \frac{-Q}{4}$
- b)  $q = \frac{Q}{4}$
- c)  $q = \frac{3Q}{4}$
- d)  $q = -\frac{3Q}{4}$

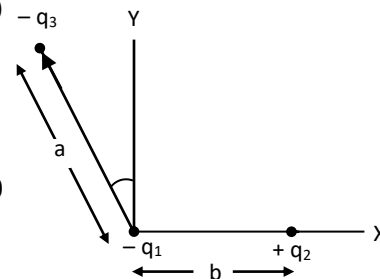


2. Two charged spheres of radius  $R_1$  and  $R_2$  respectively are charged and joined by a wire. The ratio of electric field of the spheres is

- a)  $R_1 / R_2$
- b)  $R_2 / R_1$
- c)  $R_1^2 / R_2^2$
- d)  $R_2^2 / R_1^2$

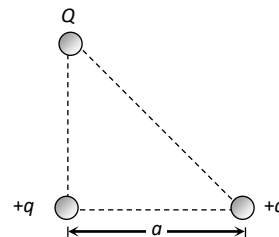
3. Three charges  $-q_1$ ,  $+q_2$  and  $-q_3$  are placed as shown in figure. The x-component of the force on  $-q_1$  is proportional to

- a)  $\frac{q_2}{b^2} - \frac{q_3}{a^2} \cos \theta$
- b)  $\frac{q_2}{b^2} + \frac{q_3}{a^2} \sin \theta$
- c)  $\frac{q_2}{b^2} + \frac{q_3}{a^2} \cos \theta$
- d)  $\frac{q_2}{b^2} - \frac{q_3}{a^2} \sin \theta$



4. Three charges  $Q$ ,  $+2q$  and  $+q$  are placed at the vertices of a right-angled isosceles triangle as shown. The net electrostatic energy of the configuration is zero if  $Q$  is equal to

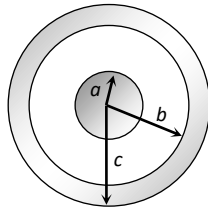
- a)  $\frac{-q}{1 + \sqrt{2}}$
- b)  $\frac{-\sqrt{2}q}{1 + \sqrt{2}}$
- c)  $-2q$
- d)  $+q$



SPACE FOR ROUGH WORK

5. A solid conducting sphere of radius  $a$  has a net positive charge  $2Q$ . A conducting spherical shell of inner radius  $b$  and outer radius  $c$  is concentric with the solid sphere and has a net charge  $-Q$ . The surface charge density on the inner and outer surfaces of the spherical shell will be

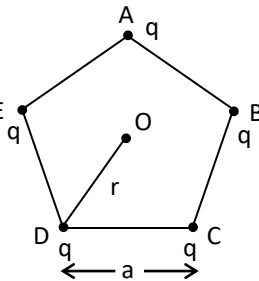
- a)  $-\frac{2Q}{4\pi b^2}, \frac{Q}{4\pi c^2}$
- b)  $-\frac{Q}{4\pi b^2}, \frac{Q}{4\pi c^2}$
- c)  $0, \frac{Q}{4\pi c^2}$
- d) None of the above



6. Five charges,  $q$  each are placed at the corners of a regular pentagon of side ' $a$ ' (Fig).

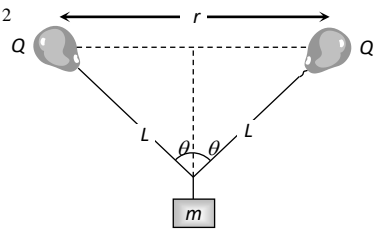
The electric field at O if the charge  $q$  at A is replaced by  $-q$  is

- a) 0
- b)  $\frac{1}{4\pi\epsilon_0} \cdot \frac{2q}{r^2}$  (along OA)
- c)  $\frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r^2}$  (along OA)
- d)  $\frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r^2}$  (away from OA)

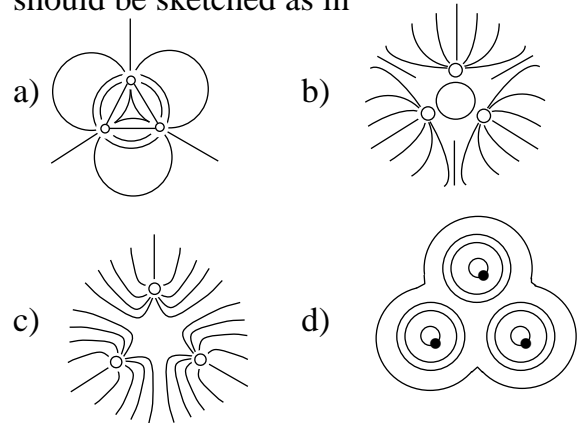


7. Two similar balloons filled with helium gas are tied to  $L$  m long strings. A body of mass  $m$  is tied to another ends of the strings. The balloons float on air at distance  $r$ . If the amount of charge on the balloons is same then the magnitude of charge on each balloon will be

- a)  $\left[ \frac{mgr^2 \tan \theta}{2k} \right]^{1/2}$
- b)  $\left[ \frac{2k}{mgr^2} \tan \theta \right]^{1/2}$
- c)  $\left[ \frac{mgr}{2k} \cot \theta \right]^{1/2}$
- d)  $\left[ \frac{2k}{mgr} \tan \theta \right]^{1/2}$



8. Three positive charges of equal value  $q$  are placed at the vertices of an equilateral triangle. The resulting lines of force should be sketched as in

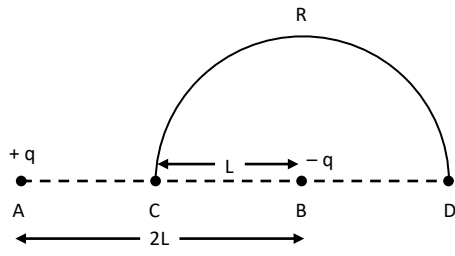


9. Two point charges  $Q$  and  $-3Q$  are placed at some distance apart. If the electric field at the location of  $Q$  is  $E$ , then at the locality of  $-3Q$ , it is

- a)  $-E$                       b)  $-3E$
- c)  $E/3$                       d)  $-E/3$

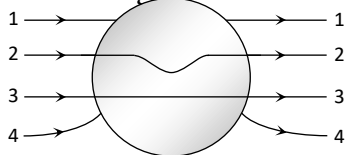
10. Charges  $+q$  and  $-q$  are placed at points A and B respectively, which are distance  $2L$  apart. C is the mid-point between A and B, fig. The work done in moving a charge  $+Q$  along the semicircle CRD is

- a)  $\frac{qQ}{2\pi\epsilon_0 L}$
- b)  $\frac{qQ}{6\pi\epsilon_0 L}$
- c)  $\frac{-qQ}{6\pi\epsilon_0 L}$
- d)  $\frac{qQ}{4\pi\epsilon_0 L}$

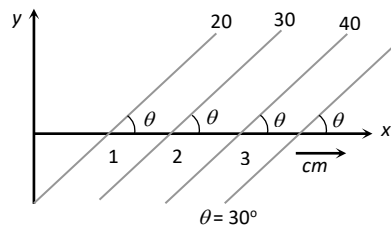


11. A metallic sphere is placed in a uniform electric field. The lines of force follow the path (s) shown in the figure as

- a) 1
- b) 2
- c) 3
- d) 4



12. Some equipotential surface are shown in the figure. The magnitude and direction of the electric field is



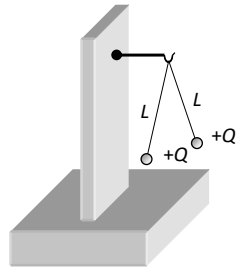
- a)  $100\text{ V/m}$  making angle  $120^\circ$  with the  $x$ -axis
- b)  $100\text{ V/m}$  making angle  $60^\circ$  with the  $x$ -axis
- c)  $200\text{ V/m}$  making angle  $120^\circ$  with the  $x$ -axis
- d) None of the above

13. An infinite number of charges, each of charge  $1\mu\text{C}$ , are placed on the  $x$ -axis with co-ordinates  $x = 1, 2, 4, 8, \dots, \infty$ . If a charge of  $1\text{ C}$  is kept at the origin, then what is the net force acting on  $1\text{ C}$  charge?

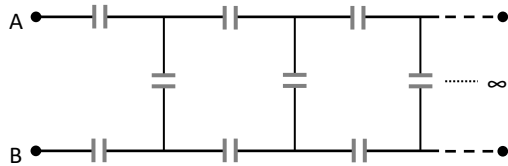
- a)  $9000\text{ N}$                       b)  $24000\text{ N}$
- c)  $12000\text{ N}$                       d)  $36000\text{ N}$

14. Two small balls having equal positive charge  $Q$  (coulomb) on each are suspended by two insulated string of equal length  $L$  meter, from a hook fixed to a stand. The whole set up is taken in satellite into space where there is no gravity (state of weightlessness). Then the angle between the string and tension in the string is:

- a)  $180^\circ, \frac{1}{4\pi\epsilon_0} \cdot \frac{Q^2}{(2L)^2}$
- b)  $90^\circ, \frac{1}{4\pi\epsilon_0} \cdot \frac{Q^2}{L^2}$
- c)  $180^\circ, \frac{1}{4\pi\epsilon_0} \cdot \frac{Q^2}{2L^2}$
- d)  $180^\circ, \frac{1}{4\pi\epsilon_0} \cdot \frac{QL}{4L^2}$



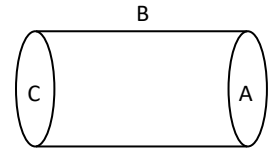
15. The equivalent capacity of the infinite network as shown if each capacitor is of  $1 \mu\text{F}$  is



- a)  $\frac{\sqrt{3}-1}{2} \mu\text{F}$
- b) infinity
- c)  $\frac{\sqrt{3}+1}{2} \mu\text{F}$
- d)  $1 \mu\text{F}$

16. A hollow cylinder has a charge  $q$  coulomb within it. If  $\phi$  is the electric flux in unit of volt metre associated with the curved surface B, the flux linked with the plane surface A in unit of volt metre will be

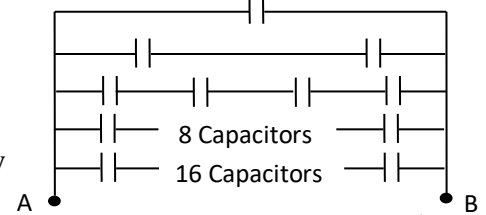
- a)  $\frac{1}{2} \left( \frac{q}{\epsilon_0} - \phi \right)$
- b)  $\frac{q}{2\epsilon_0}$
- c)  $\frac{\phi}{3}$
- d)  $\frac{q}{\epsilon_0} - \phi$



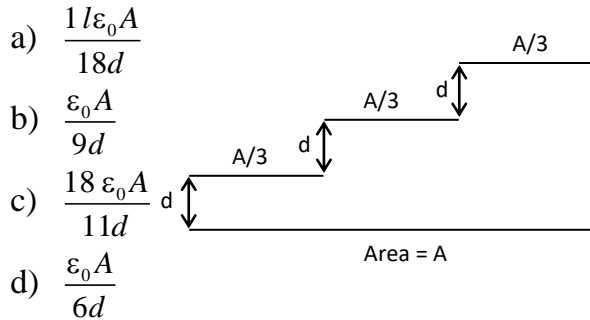
17. The electric field intensity between the two plates of the capacitor is  $\frac{1}{\sqrt{8.85}} \times 10^2$  V/m. If the dielectric constant of the medium between the two plates is 4, the energy density of the medium is:
- a)  $40000 \text{ J/m}^3$
  - b)  $80000 \text{ J/m}^3$
  - c)  $60000 \text{ J/m}^3$
  - d)  $2 \times 10^{-8} \text{ J/m}^3$

18. An infinite number of identical capacitors each of capacitance  $1 \mu\text{F}$  are connected as shown in adjoining figure. The equivalent capacitance between A and B is:

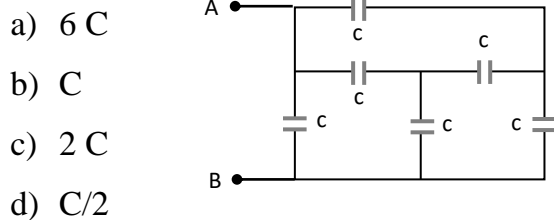
- a)  $1 \mu\text{F}$
- b)  $2 \mu\text{F}$
- c)  $1/2 \mu\text{F}$
- d) infinity



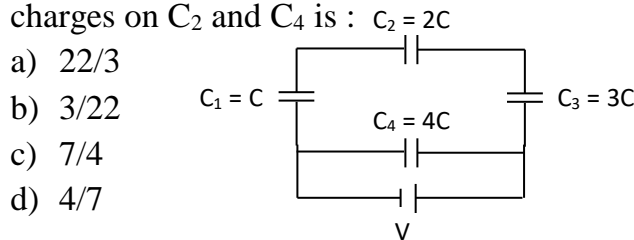
19. A capacitor is made of plate of area  $A$  and a second plate having a stair – like structure as shown in figure. If the width of each stair is  $A/3$  and the height is  $d$ , find the capacitance of the arrangement.



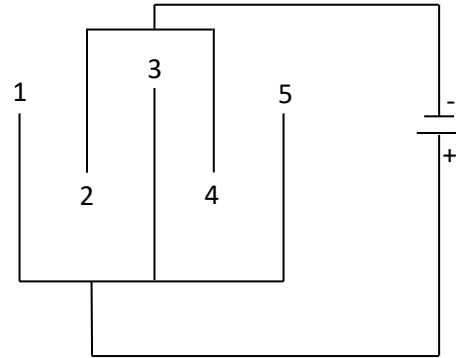
20. Six equal capacitors each of capacitance  $C$  are connected as shown in the figure below. Then the equivalent capacitance between A and B is



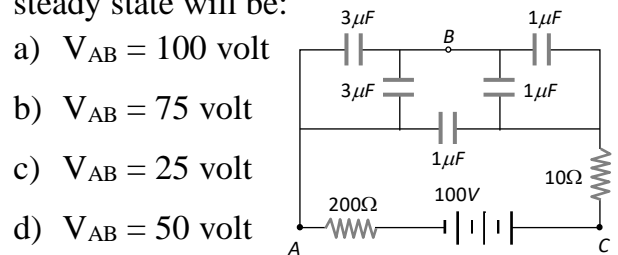
21. A network of 4 capacitors of capacity equal to  $C_1 = C$ ,  $C_2 = 2C$ ,  $C_3 = 3C$  and  $C_4 = 4C$  are connected in a battery as shown in the figure. The ratio of the charges on  $C_2$  and  $C_4$  is :



22. Five identical plates each of area  $A$  are joined as shown in the figure. The distance between the plates is  $d$ . The plates are connected to a P.D. of  $V$  volts. The charge on the plates 1 and 4 will be :



23. The potential difference between the points A and B in the following circuit in steady state will be:



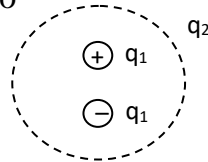
24. An electrical technician requires a capacitance of  $2 \mu F$  in a circuit across the

potential difference 1 kV. A large number of  $1 \mu\text{F}$  capacitors are available to him each of which can withstand a potential difference of not more than 300 volt. How many minimum numbers of capacitors are required to get  $2 \mu\text{F}$  capacitor?

- a) 32
- b) 18
- c) 16
- d) 2

25. Consider the charge configuration and a spherical Gaussian surface as shown in Fig. When calculating the flux of the electric field over the spherical surface, the electric field will be due to

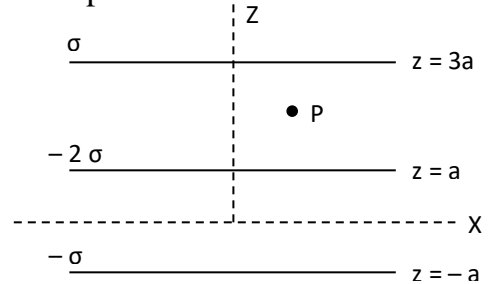
- a)  $q_2$
- b) only the positive charges
- c) all the charges
- d)  $+q_1$  and  $-q_1$



26. Electric field at a distance of  $R$  from the surface of a charged sphere of radius  $R$  and surface charge density  $\sigma$  is  $E$ . Electric field at a distance of  $R$  from the surface of a charged sphere of radius  $2R$  and surface charge density  $\sigma$  is:

- a) zero
- b)  $E$
- c)  $16E/9$
- d)  $4E/9$

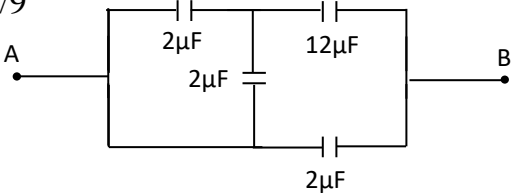
27. Three infinitely long charges sheets are placed as shown in figure. The electric field at point  $P$  is



- a)  $\frac{2\sigma}{\epsilon_0} \hat{k}$
- b)  $-\frac{2\sigma}{\epsilon_0} \hat{k}$
- c)  $\frac{4\sigma}{\epsilon_0} \hat{k}$
- d)  $-\frac{4\sigma}{\epsilon_0} \hat{k}$

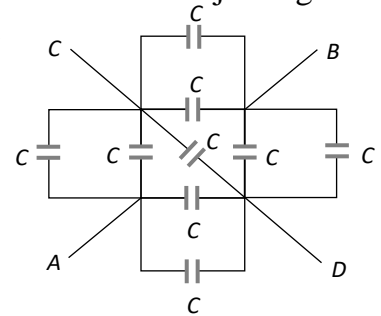
28. Four condensers are connected as shown in the figure. The effective capacity in  $\mu\text{F}$  between the points  $A$  and  $B$  are :

- a)  $28/9$
- b) 4
- c) 5
- d) 18



29. The equivalent capacity between the points  $C$  and  $D$  in the adjoining circuit (Fig) will be

- a)  $C$
- b)  $2C$
- c)  $3C$
- d)  $4C$



30. Three concentric metallic spherical shells of radii  $R, 2R, 3R$  are given charges  $Q_1, Q_2, Q_3$  respectively. It is found that the surface charge densities on the outer surfaces of the shells are equal. Then, the ratio of the charges given to the shells,  $Q_1 : Q_2 : Q_3$  is
- a)  $1 : 2 : 3$                       b)  $1 : 3 : 5$   
 c)  $1 : 4 : 9$                         d)  $1 : 8 : 18$

31. Two pith balls carrying equal charges are suspended from a common point by string of equal length; the equilibrium separation between them is  $r$ . Now the strings are rigidly clamped at half the height. The equilibrium separation between the balls now become

- a)  $\frac{1}{\sqrt{2}} \frac{r}{\epsilon_0 \epsilon_r}$   
 b)  $\frac{r}{\sqrt{3}} \frac{q^2}{\epsilon_0 \epsilon_r}$   
 c)  $\frac{2r}{\sqrt{3}} \frac{q^2}{\epsilon_0 \epsilon_r}$   
 d)  $\frac{2r}{3} \frac{q^2}{\epsilon_0 \epsilon_r}$

